

# PIV measurements of a shock-accelerated fluid instability

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## ABSTRACT

A varicose-profile, thin layer of heavy gas ( $\text{SF}_6$ ) in lighter gas (air) is impulsively accelerated by a planar, Mach 1.2 shock, producing Richtmyer-Meshkov instability. We present the first measurements of the circulation in the curtain during the vortex-dominated, nonlinear stage of the instability evolution. These measurements, based on particle image velocimetry data, are employed to validate an idealized model of the nonlinear perturbation growth.

**Keywords:** Richtmyer-Meshkov, shock, instability, fluid, particle image velocimetry

## 1. INTRODUCTION

In this study, we present experimental measurements of the circulation in a shock-accelerated thin layer of  $\text{SF}_6$  gas embedded in air (i.e. gas curtain). With these measurements, we validate an inviscid, point-vortex model of nonlinear gas-curtain instability growth<sup>1</sup> by comparing our results with its predicted parameter, the circulation of the vortex cores. This is the first time that the circulation derived from a simple model of mixing width growth has been compared to a measured value of circulation. This comparison provides the connection among an inviscid model, traditional integral measurements of the mixing-layer width, and detailed velocity-field measurements.

Richtmyer-Meshkov instability (RMI) developing on shock-accelerated, perturbed density interfaces goes through several stages of evolution before eventual transition to turbulence.<sup>2</sup> The initial, linear growth stage was first theoretically described by Richtmyer.<sup>3</sup> Subsequently, the instability grows in a nonlinear manner, and the flow is dominated by the vortices created by the initial baroclinic vorticity generation. Several theoretical models have been developed to describe this nonlinear region of the instability's development.<sup>1,4-7</sup> Only measurements of large-scale features of the flow have been available to validate those growth models up to now. While our present findings describe the second stage of the curtain evolution (nonlinear, vortex-dominated growth), the same experimental technique applied at later times can produce quantitative information about the transition to turbulence.

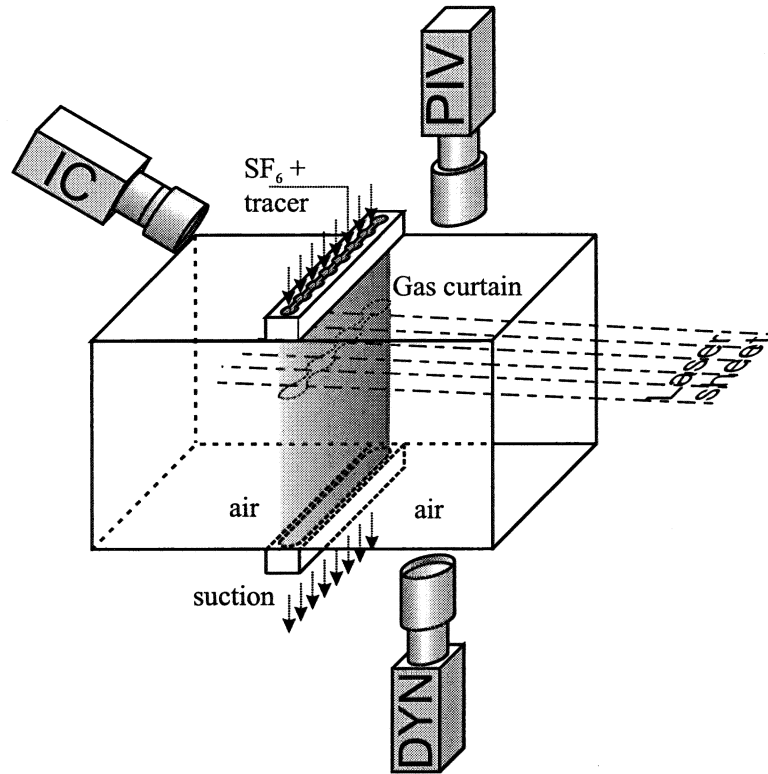
We study the development of the interfaces of a perturbed curtain (i.e. thin layer) of heavy gas ( $\text{SF}_6$ ) embedded in ambient air when the curtain is accelerated by a Mach 1.2 normal shock created in a horizontal shock tube. The shock-tube facility is the same as that used in earlier experiments,<sup>8-10</sup> except for the improved diagnostics. The current experimental configuration will be described in detail elsewhere.<sup>11</sup>

The test section of the shock tube (75 mm square) is shown in Fig. 1. A laminar curtain of  $\text{SF}_6$  is injected through a contoured nozzle vertically into the top side of the test section and removed on the bottom side. The nozzle profile imposes a varicose perturbation with dominant wavelength  $\lambda = 6$  mm on the curtain. The  $\text{SF}_6$  is seeded with small ( $d \leq 0.5 \mu\text{m}$ ) glycol/water droplets from a theatrical fog generator which allow us to make the particle image velocimetry (PIV) measurements. See Refs.<sup>2</sup> and<sup>11</sup> for detailed analyses which show that the fog particles accurately track the  $\text{SF}_6$  curtain. The tube creates high quality planar shocks of Mach 1.2 that propagate through the test section and accelerate the curtain.

The gas curtain is illuminated using two frequency-doubled, pulsed Nd:YAG lasers, the first of which is a customized, burst-mode laser that is configured to fire seven pulses (100-ns duration, 3 mJ) spaced 140  $\mu\text{s}$  apart. The second is a commercial 10 Hz laser (New Wave Research Minilase-20) with a 10-ns, 10-mJ pulse, which is fired once per event. The light from both lasers is focused into coplanar, horizontal sheets in the test section, as shown in Fig. 1, and three single-frame, gated, intensified CCD cameras by Hadland Photonics (model SV-533 BR, 1134  $\times$  468 pixels) look at fixed, preset fields of view. The "IC" camera records the image of the initial conditions on one

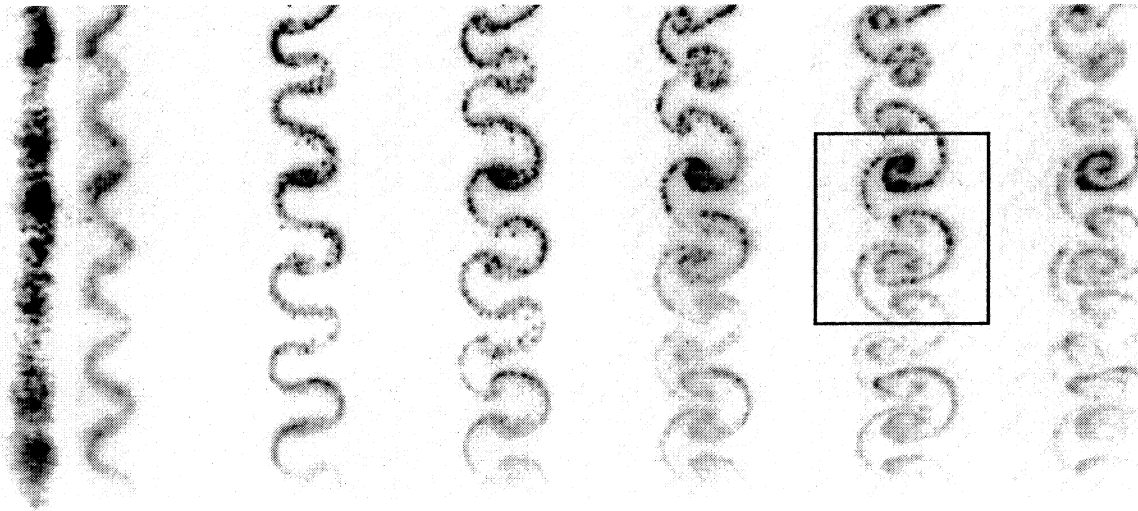
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**Figure 1.** Shock tube test section (shock propagates from left to right).

frame, while the “Dynamic” (“DYN” in Fig. 1) camera observes the rest of the test section to capture multiple exposures of the gas curtain as it is advected downstream. The large freestream velocity causes all of the images to be physically separated on the CCD. The “PIV” camera focuses on a small region of the dynamic field, about 19 by 14 mm, to detect the individual fog droplets.

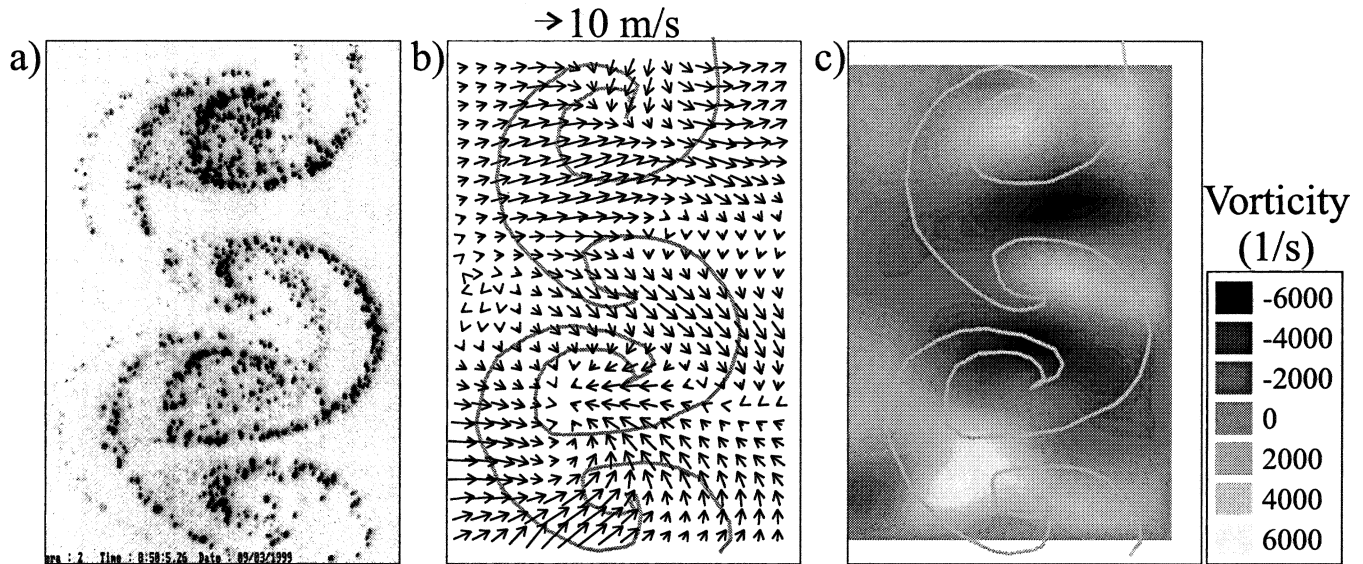


**Figure 2.** Initial conditions ( $t = 0$ ) and dynamic images at  $t = 120, 260, 400, 540, 680$  and  $820 \mu\text{s}$  after shock interaction. Region imaged by PIV camera is inside black rectangle.

An image with the view of the initial conditions and the dynamic image from the IC and “Dynamic” cameras is

shown in Fig. 2. The actual image from the PIV camera is double-exposed, first from the burst-mode laser at 680  $\mu\text{s}$ , and then from the single-pulse laser at 698.4  $\mu\text{s}$ . The latter is not recorded by the “Dynamic” camera because the camera intensifier is gated off during the second pulse.

The negative of the image captured by the PIV camera is shown in Fig. 3a. Visible in the figure is the double exposure caused by the two different laser pulses, separated by 18.4  $\mu\text{s}$ . We will use the downstream-pointing mushroom structure in the middle of the image to illustrate the process of determining mixing width and circulation in the flowfield. Fig. 3b is the velocity field created by performing single-frame cross-correlation on the image in Fig. 3a. We take the velocity field to be representative of a time midway between the two exposures of Fig. 3a, at 689.2  $\mu\text{s}$  after shock impact. The measured freestream velocity of 97 m/s has been subtracted from the field. From this



**Figure 3.** PIV measurements. (a) Region captured by the PIV camera. (b) Velocity field corresponding to the image (a). (c) Vorticity isocontours. The gray line in (b) and (c) shows the position of the curtain midway between the two exposures of (a).

velocity field, a vorticity field is created by calculating the circulation around each vector using the eight surrounding vectors<sup>12</sup>; this is shown in Fig. 3c. What becomes apparent is that each roll-up region at the intersection of the mushroom “stem” and “cap” in Fig. 3a corresponds to a concentration of vorticity, and there is a pair of counter-rotating vortices matching each mushroom. We expect this from observations of the image, and it is confirmed by the PIV measurements. The alternating signs of vorticity caused by the symmetric mushroom structures are clear in the figure.

Using this new flow-field information contained within the large-scale structures, we can now compare the circulation determined from an inviscid growth model with that measured using PIV. Let us first briefly summarize the important features of the model for the growth of the mixing region.<sup>1,10</sup>

The model is based upon an infinite row of counter-rotating point vortices, approximating the vorticity which is baroclinically generated on the interfaces between the heavy and light gases when the shock impacts the curtain. Each vortex has the same circulation,  $\Gamma$ , and there is one local wavenumber associated with the flow,  $k$ , where  $k = 2\pi/\lambda$ . For the single-mode nozzle used in these experiments,  $\lambda = 6$  mm, and  $k$  was set at a fixed value of 1.04  $\text{mm}^{-1}$ . The expression for the growth of the mixing region in time is<sup>1,10</sup>:

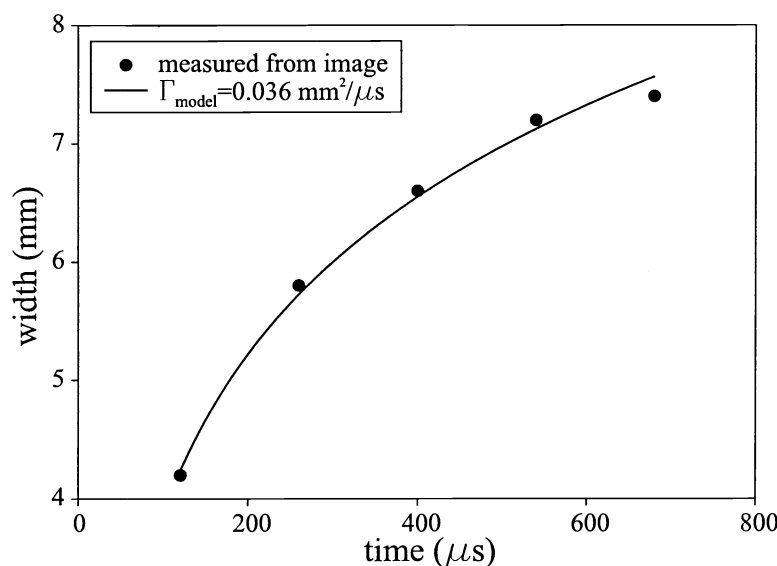
$$w(t) = \frac{2}{k} \sinh^{-1} \left( k^2 \Gamma (t - t_0) + \sinh \left( \frac{k w_0}{2} \right) \right), \quad (1)$$

where  $t_0$  is the virtual origin and  $w_0$  is the curtain width just after it has been compressed by the shock. This value is estimated to be  $w_0 = w_{init}/1.34$ , where the measured thickness is divided by the shock compression factor for a Mach 1.2 normal shock. The virtual origin  $t_0$ , absent from the original model,<sup>1</sup> is introduced to account for the phase

inversion of one of the interfaces.<sup>13,10</sup> Eq. 1 produces a growth rate prediction similar to other nonlinear-growth theories.<sup>6,7</sup>

Previous analysis quantified the initial thickness and temporal growth of the layer,<sup>10</sup> but the actual circulation of the flow could not be measured. We will continue with the example of Figs. 2 and 3, and illustrate how we measure the growth of the mixing region in the gas curtain and determine the circulation corresponding to the middle mushroom. To preserve the local flow information, we measured the individual widths corresponding to the wavelength along which the center mushroom appeared.

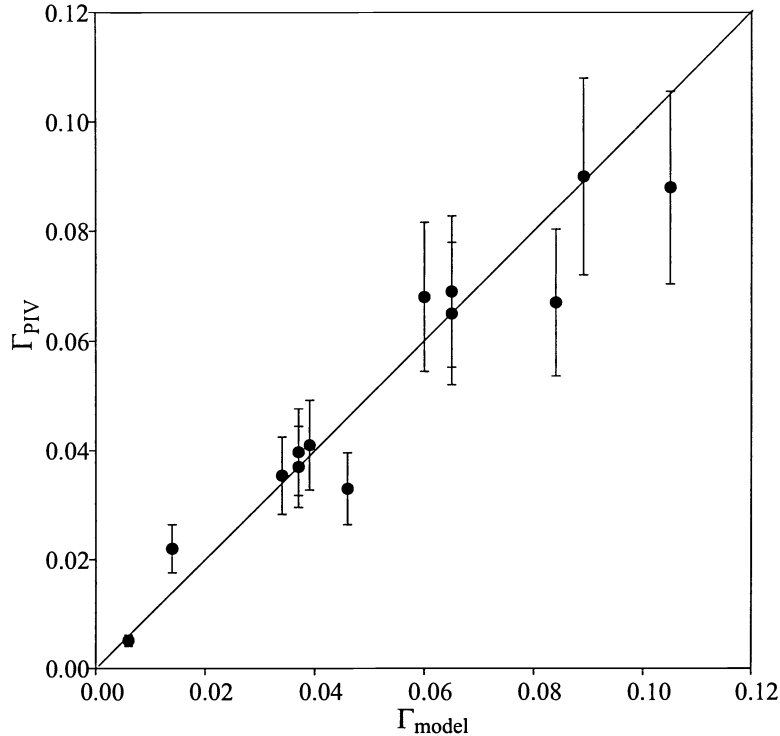
The mixing width evolutions from Fig. 2 for mushrooms A and B are plotted in Fig. 4. It is immediately apparent that the mixing widths corresponding to each mushroom are very similar. Using  $\Gamma$  and  $t_0$  as free parameters, where  $w_0$  and  $k$  are fixed parameters measured from the initial conditions, the  $w(t)$  data are fit to Eq. 1 (these fits are also shown in Fig. 4). The value  $k$  remains nearly constant during instability growth, even though mushroom orientation varies. The model from Eq. 1 converges with a residual,  $r^2$ , of 0.99, where  $r^2 = 1.0 - \sum_{i=1}^n [(w_{fit} - w_i)^2 / (w_i - \bar{w})^2]$  and  $\bar{w}$  is the average width of the curtain. The curve fit gives us a circulation for the mushroom, such that  $\Gamma_{model} = 0.036 \text{ mm}^2/\mu\text{s}$ .



**Figure 4.** Curve fit using the growth model in Eq. 1. Symbols are experimental data, line is curve fit. Error bars on data points are no larger than the points.

To validate the model in Eq. 1, we compare the circulation from the curve fit of Fig. 4 to the vorticity field of Fig. 3c. The circulation from the PIV data was calculated by drawing a closed curve around the region of negative vorticity corresponding to the middle mushroom and computing the line integral of tangential velocity around the entire curve. This process yields circulation:  $\Gamma_{PIV} = 0.035 \text{ mm}^2/\mu\text{s}$ . We measured  $\Gamma$  with the curve-fitting and PIV procedures for other data sets, and the comparison between  $\Gamma_{PIV}$  and  $\Gamma_{model}$  is shown in Fig. 5. The range of circulation values from 0.01 to  $0.11 \text{ mm}^2/\mu\text{s}$  is caused by uncontrolled but carefully measured variations in the initial state of the varicose interface. The agreement shown in Fig. 5 is quite good, with over two-thirds of the data within an error bar of the fit,  $\Gamma_{PIV} = \Gamma_{model}$ . Thus, the model (Eq. 1) is a reliable estimator of mixing width during this phase of the instability. It is also noteworthy that the delay,  $t_0$ , recovered by the curve-fit varied from 0 to  $60 \mu\text{s}$ , which is consistent with the duration of the phase inversion observed in our experiments.<sup>14</sup>

Several physical effects contribute to observed differences. The model assumes an initially sharp interface, but the actual interface is diffuse.<sup>10,11</sup> Also, mode-coupling, not included in the model, is beginning at the time of the PIV measurements. For several events in Fig. 5 the counter-rotating vortices are not perfectly aligned in the spanwise direction, as assumed by the model. The correlation of  $\Gamma$  values shown in Fig. 5 is quite good despite these limitations, which suggests that the inviscid vortex dynamics driving the instability are fairly robust, and that dissipation is negligible.



**Figure 5.** Comparison between the circulation measured using PIV and the circulation from the curve fits of Eq. 1 of mixing width growth for many experiments similar to the one in Fig. 3. Error bars represent PIV measurement uncertainty.

In summary, we have shown that there is agreement between the circulations determined directly from PIV measurements and the circulations deduced from curve fits of the model represented by Eq. 1 to measured mixing width data. Thus, the growth of the curtain with a single, dominant wavelength during the period of nonlinear, vortex-dominated evolution can be modeled using inviscid mechanisms in the regime which we have examined ( $t < 1$  ms). Under these flow conditions, there is little apparent dissipation of the initial vorticity deposited in the gas curtain by the shock, as indicated by the close match between the circulation of the idealized model and the circulation calculated from the velocity-field measurements. For the first time, we have been able to make a strong correlation between the circulation predicted from integral measurements of the mix layer and the actual circulation of the large-scale vortex structures within the layer.

## ACKNOWLEDGMENTS

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